

Composition and Decomposition of Functions

1. $f(x) = x^2 - 3x + 5$ and $g(x) = 2x - 7$

A. Find $(f \circ g)(x)$.

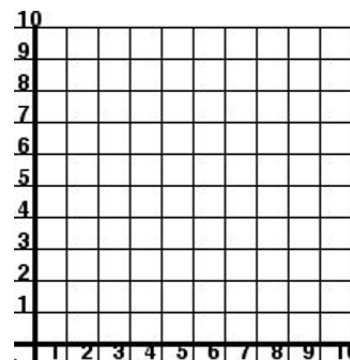
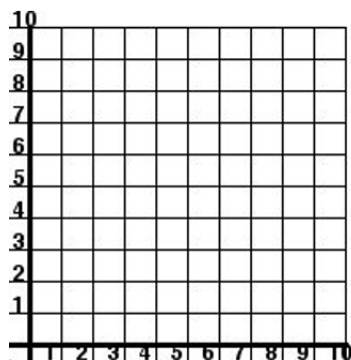
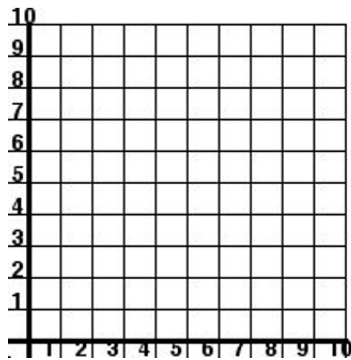
B. Find $(g \circ g)(-4)$.

2. The number N of bacteria in a refrigerated food is given by $N(T) = 20T^2 - 80T + 500, 2 \leq T \leq 14$
Where T is the temperature of the food in degrees C.

When the food is removed from refrigeration, the temperature of the food is given by $T(t) = 4t + 2, 0 \leq t \leq 3$
Where t is the time in hours.

- (A) Find the composition of $(N \circ T)(t)$ and interpret its meaning in this context.
- (B) Find the bacteria count after 1.5 hours.
- (C) Find the time when the bacteria count reaches 2000.

- 3.
- A. Use the graphs of f and $(f + g)$ to make a table showing the values of $g(x)$ when $x = 1, 2, 3, 4, 5$ and 6. Explain your reasoning.
- B. Use the graphs of f and $(f - h)$ to make a table showing the values of $h(x)$ when $x = 1, 2, 3, 4, 5$ and 6. Explain your reasoning.



4. Find two functions f and g such that $(f \circ g)(x) = h(x)$.

$$h(x) = (2x + 1)^2$$

5. Find two functions f and g such that $(f \circ g)(x) = h(x)$.

$$h(x) = (1 - x)^3$$

6. Find two functions f and g such that $(f \circ g)(x) = h(x)$.

$$h(x) = \frac{1}{x + 2}$$

7. Find two functions f and g such that $(f \circ g)(x) = h(x)$.

$$h(x) = \frac{4}{(5x + 2)^2}$$

8. Find two functions f and g such that $(f \circ g)(x) = h(x)$.

$$h(x) = 9x^2 + 6x + 3$$

9. Find two functions f and g such that $(f \circ g)(x) = h(x)$.

$$h(x) = \frac{27x^3 + 6x}{10 - 27x^3}$$