$\qquad$ Date $\qquad$ Period $\qquad$

## Without a calculator:

1. Evaluate the expression without using a calculator (you must show your work).

| A. | B. <br> $\log 10$ | C. <br> $\log _{b} b^{-3}$ | D. <br> $\log _{9} 243$ | E. <br> $\log _{5}-25$ | F. <br> $\log _{7} \sqrt[3]{49}$ | G. <br> $\log _{4} 2+\log _{4} 32$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |

2. Rewrite the equation in exponential form.

| A. | B. <br> $\log _{3} 81=4$ | C. <br> $\log _{\frac{1}{2}} 8=-3$ | D. <br> $\log _{9} 3=\frac{1}{2}$ |
| :--- | :--- | :--- | :--- |

3. Choose from the functions below to match the graphs without a calculator.

| A. | B. | C. | D. | F. |
| :--- | :--- | :--- | :--- | :--- | :--- |

A)

B)

D)

E)

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| :---: |
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4. Use a calculator to evaluate the logarithm. Round to three decimal places.
a) $\log 145$
b) $2 \ln 0.75$
c) $\log _{3} 17$
d) $\quad \log _{5} \frac{1}{4}$
5. Complete the table for a savings account in which interest is compounded continuously. Round to two decimal places.

| Initial investment | Annual \% Rate | Time to Double | Amount after 10 years |
| :--- | :--- | :--- | :--- |
| $\$ 30,000$ | $8.5 \%$ |  |  |
| $\$ 15,000$ |  | $16 y e a r s$ |  |

6. Expand completely:

| A. | B. |  |
| :--- | :--- | :--- |
| $\log 4 x^{5} \frac{8 x^{2}(y-2)}{\sqrt{z}}$ |  | C. |
| $\ln \sqrt{x} y^{3}$ |  |  |

7. Condense completely:

| A. | B. |  |
| :--- | :--- | :--- |
| $4[\ln z+\ln (z+5)]-2 \ln (z-5)$ | $\log _{5} 8-\log _{5} x$ | C. |
| $3 \ln x+4 \ln y-4 \ln z$ |  |  |

8. Solve for x in each equation

| A. | B. <br> $2^{x+2}=32$ <br> $2^{x}=20$ | C. <br> $2\left(4^{2 x-8}\right)-5=27$ |
| :--- | :--- | :--- |
| D. $\ln (11-6 x)=\ln (1-x)$ | E. $\log _{4} x=-2$ | F. $15 \ln x=45$ |
| H. $2 \log _{3} 5 x=20$ | I. $\log _{2} x+\log _{2}(x+2)=\log _{2}(x+6)$ | J. $\log _{3} x+\log _{3}(x-8)=2$ |
|  |  |  |

9. Calculate the amount if $\$ 10,000$ is invested at $3.75 \%$ interest for 40 years. Compare the results and determine which is a better deal.
a) compounded monthly
b) compounded continuously
10. A sum of $\$ 12,000$ is invested at a rate of $7.55 \%$ compounded continuously. How long will it take to double?
11. The number of bacteria N in a culture is modeled by $\mathrm{N}=$ $200 \mathrm{e}^{\mathrm{kt}}$ where t is the time in hours. If $\mathrm{N}=800$ when $\mathrm{t}=4$, estimate the time required for the population to double in size. Solve the equation. (first solve for k ). Round to three decimal places if needed.
E. 12. The population of Tucson is 515,526 , which can be model with $\mathrm{P}=515,526 \mathrm{e}^{0.012 t}$ where $\mathrm{t}=0$ represents the year 2009. According to this model, in what year will the population reach 570,000 ?
12. Find the exponential equation for each graph in the form $f(x)=c\left(b^{x}\right)$
A.

B.

13. Sketch the graph of each function. State the shifts, domain, range, intercepts and asymptotes of each.
A. $g(x)=\log _{4}(x+2)+4$

B. $f(x)=-2^{x-1}-3$

14. Find the zeros of the polynomial
$f(x)=12 x^{3}+11 x^{2}-13 x-10$
15. If $(\mathrm{x}-8 \mathrm{i})$ is a factor of a polynomial, what is another factor? Write a possible equation in standard form that would give the zeros associated with those factors.
16. Sketch a polynomial with the following:

- Positive lead coefficient
$\mathrm{x}=2$ with multiplicity 3
$\mathrm{x}=5$ with multiplicity 1
$\mathrm{x}=-3$ with multiplicity 2


18. Find the intercepts, asymptotes, domain and range of the rational function. Sketch a graph of the function.
$f(x)=\frac{x^{2}-5 x+4}{x^{2}-4}$
Intercepts
x-intercept(s)
y-intercept

## Asymptotes

Horizontal:
Vertical:
Slant:

## Domain

D :


## Hole:

